

Dynamics of Machines

Basic Definitions

Kinematics: Study of motion without considering the causes of motion.

Dynamics: " " white "
 " " - - -

Statics : Study of ~~bodies~~ and forces in a stationary mechanical system

Mechanism: Arrangement of bodies and joints to transmit motion

Machine:

Primary engineering purpose. For example
regulator in a watch: mechanism
stone crusher } machine
arm of loader }

→ **Arrangement:** A thoughtful (logical) process of creating a mechanism/machine
↳ Synthesis / Design

Machine = bodies + joints

↓
links
(rigid)

↓
?

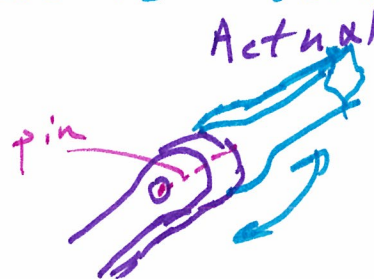
Joint: A device that allows a specific relative motion between two links

Examples:

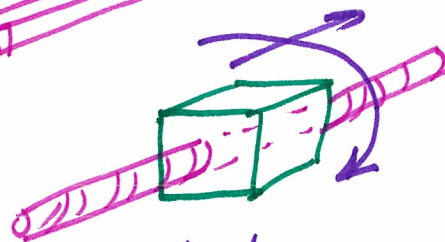
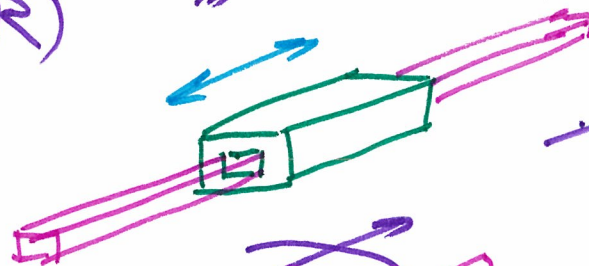
Hinge
Revolute (R)

Prismatic
(P)

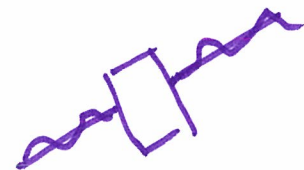
Helical
(H)



schematic



translation is
function of
the rotation

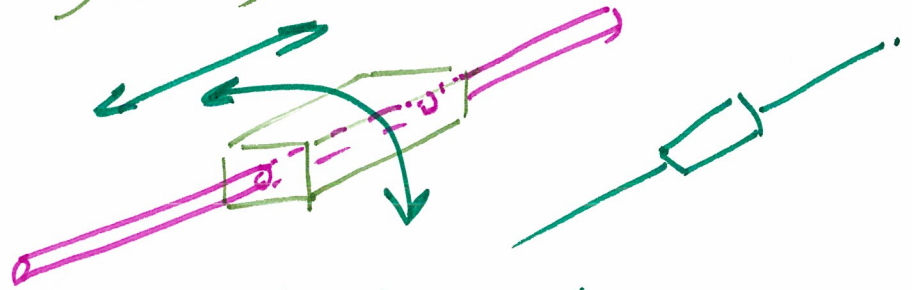


Allow one type of motion only

↳ 1 Degree of Freedom (DOF)

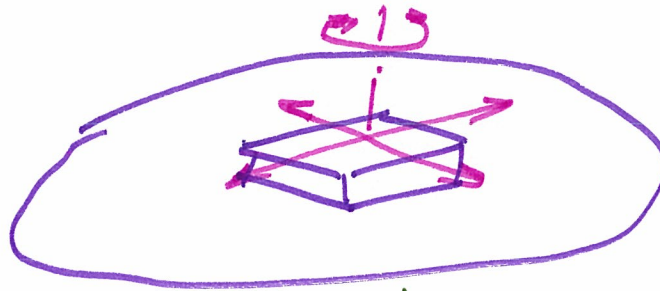
2 DOF joints

Cylindrical
(C)

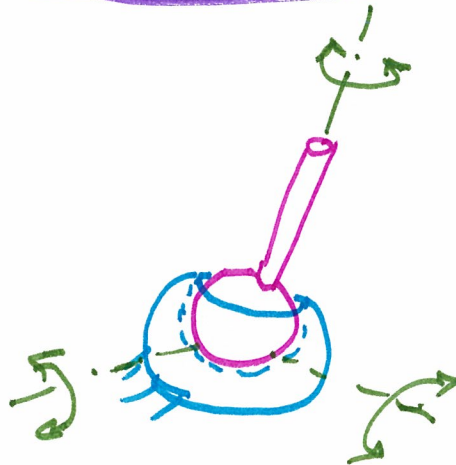


rotation & translation
are independent

3 DOF
Planar
(P)

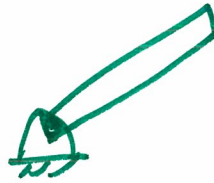


Spherical
(S)

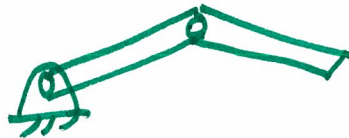


Create Mechanisms/Machines as sequence of joints

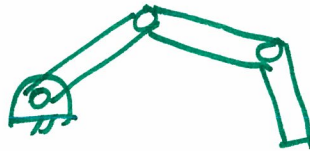
R



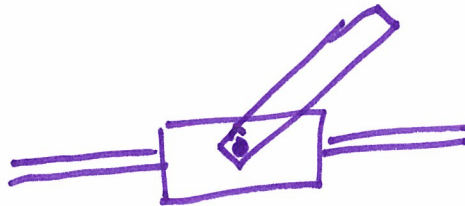
RR



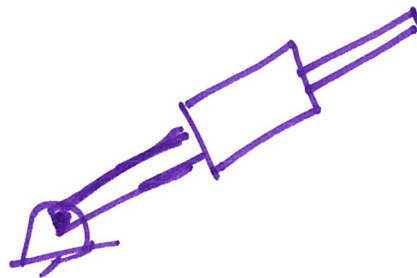
RRR



PR



RP



Example:

Motorcycle suspension (rear tire)



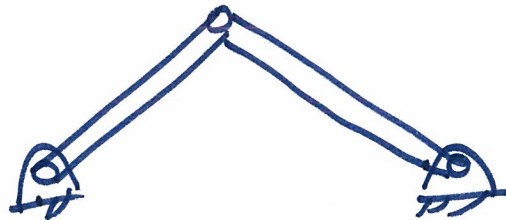
RRPR

Estimate the degree of freedom
by inspecting a system

Example

RRR

DOF = 0



Open-loop mechanisms

Closed-loop "

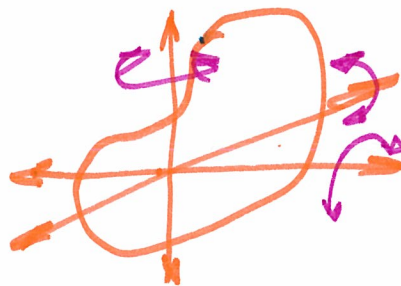
Ground: reference link, which is typically
fixed

Calculating Mobility (DOF)

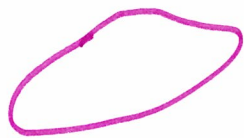
Start with general case & go to special (planar)
(3D space)

Observation:

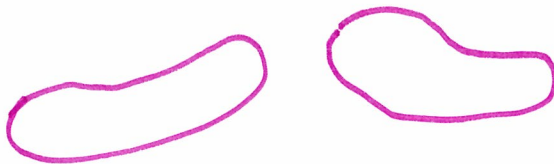
A body (link) has 6 DOF in space



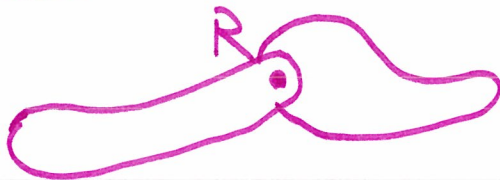
3 translation
3 rotations



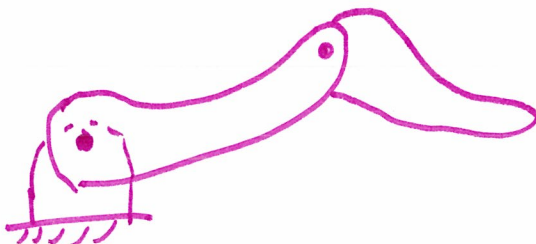
$$M = 6$$



$$M = 2(6) = 12$$



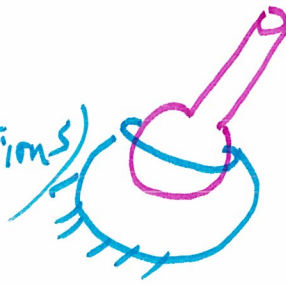
$$M = 2(6) - 5 = 7$$



$$M = 2(6) - 2(5) = 2$$

$$M = 6 - 3$$

(lost 3 translations)



Gruebler Criterion

$$M = 6(L - 1) - 5J_1 - 4J_2$$

↓
number
of links
including
the ground

↓
joint
with
1 DOF

↓
Joint
with
2 DOF

Special case Planar

Links have 3 DOF

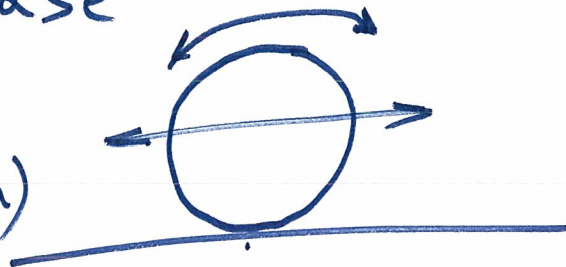
$$M = 3(L - 1) - 2J_1 - J_2$$

Important case

Wheel

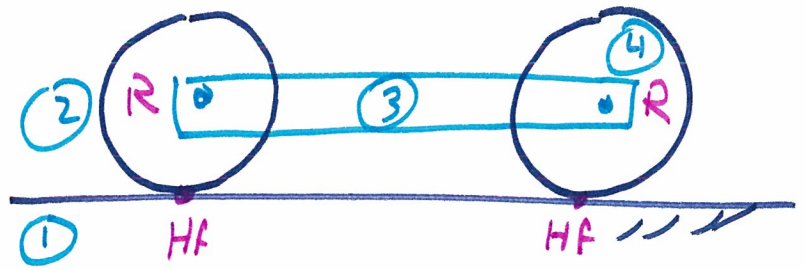
(in planar motion)

Half joint



Example

M?



$$M = 3(L - 1) - 2J_1 - J_2$$

$$= 3(4 - 1) - 2(2) - 2$$

$$= 9 - 4 - 2$$

$$= 3 \rightarrow \text{makes sense?}$$

↳ translation
spinning of (2)
" of (4)

Steps:

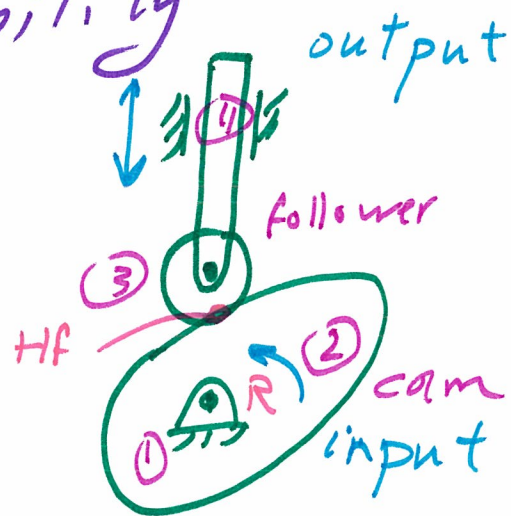
- label links

- label joints

Notes on Mobility

Cam

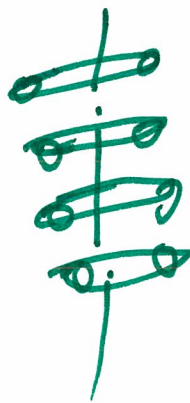
1 & 2	R
2 & 3	HF
3 & 4	R
4 & 1	P



$$M = 3(4-1) - 2(3) - 1$$

$$= 9 - 6 - 1 = 2 \rightarrow \text{oscillation of (4)} \\ \text{spining of (3) in place}$$

Spring



=



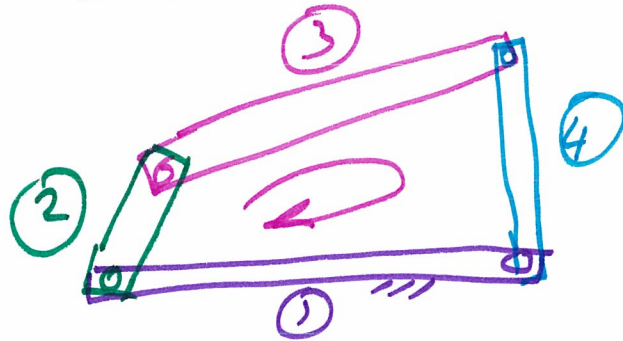
replace by two
links joined by
a Prismatic (P)
joint

Commonly Used Mechanisms (Machines)

4-Bar Mechanism

RRRR

Closed-Loop
mechanism

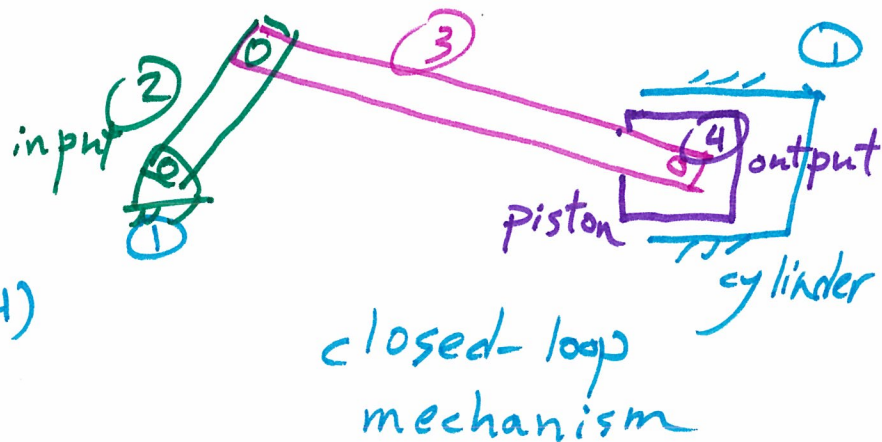


$$M = 3(4-1) - 2(4) \\ = 1$$

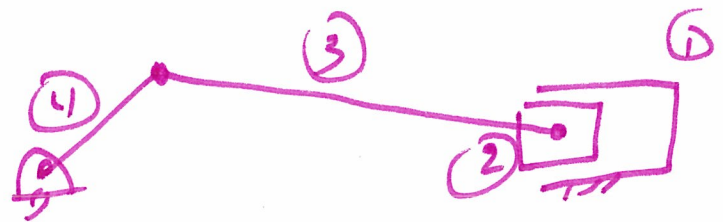
Crank-Slider (compressor)

RRRT

$$M = 3(4-1) - 2(4) \\ = 1$$



Engine PRRR

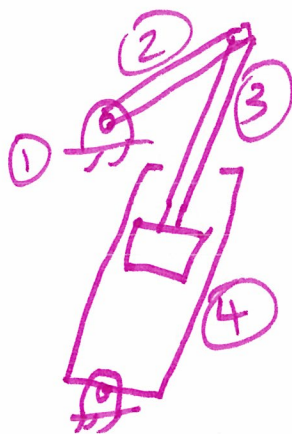


Example

Given

RRPR

$$M = 3(4-1) - 2(4) - 0 = 1$$

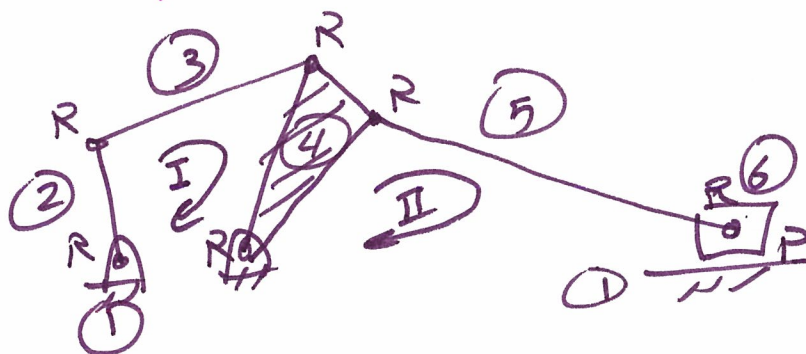


①	②	R
②	③	R
③	④	P
④	①	R

↑ Single-loop mechanisms



Multiple-loop mechanisms

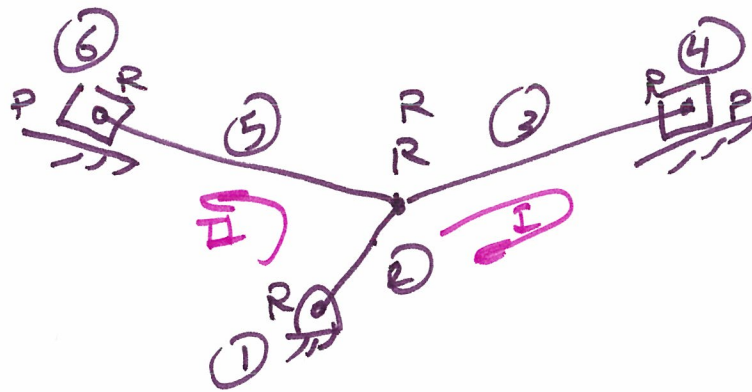


series

RRRRRR RP

$$M = 3(6-1) - 2(7) - 0 = 15 - 14 = 1$$

Parallel loops



RRRRRP RP

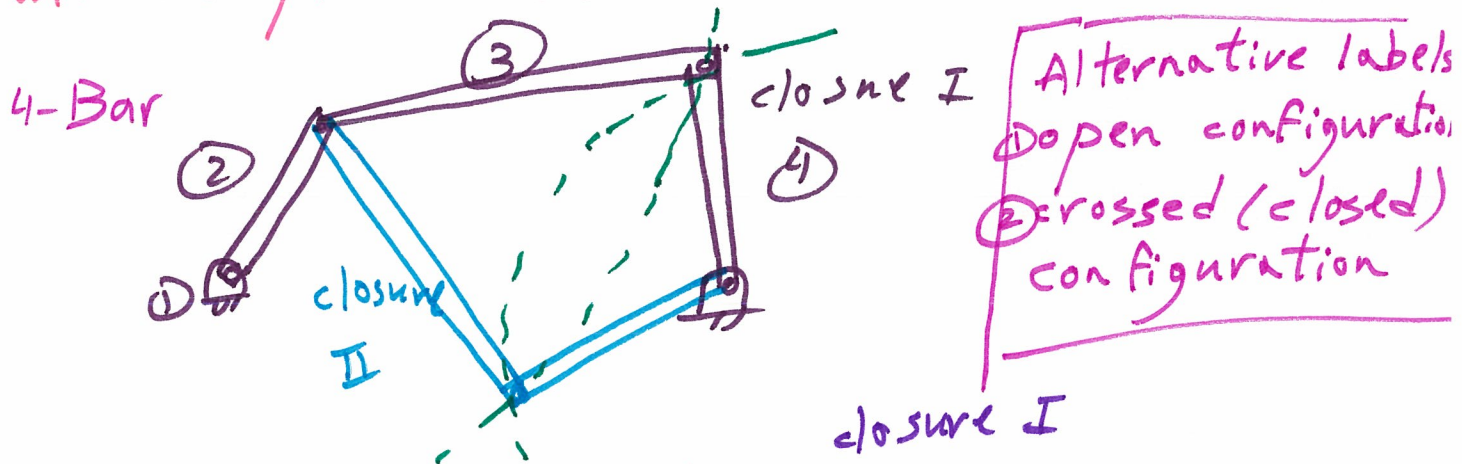
$$M = 3(6-1) - 2(7) - 0 = 1$$

①	②	R
②	③	R
③	④	R
④	①	P
②	⑤	R
⑤	⑥	R
⑥	①	P

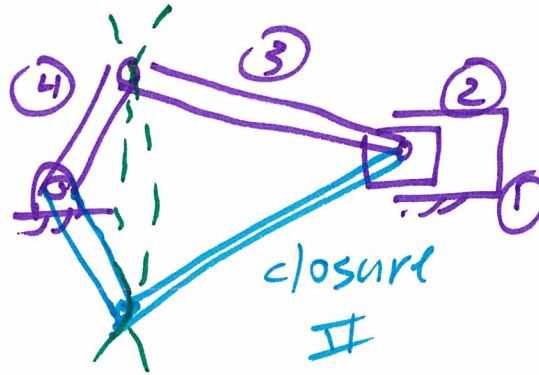
Closures:

How many ways you can assemble a mechanism while the input link is at the same position

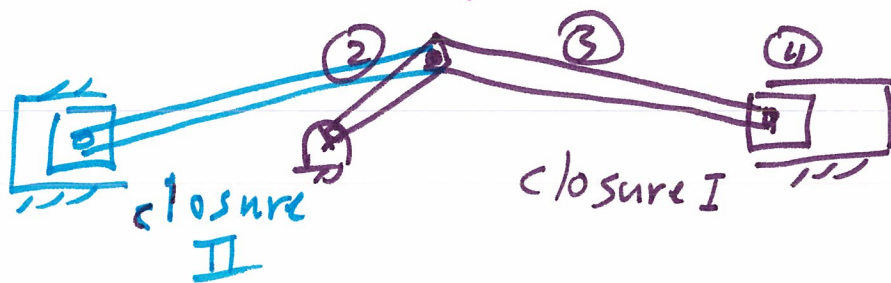
This can be useful if the machine will be placed in a crowded environment



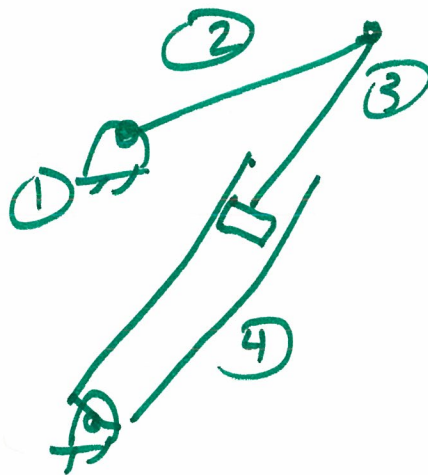
Engine



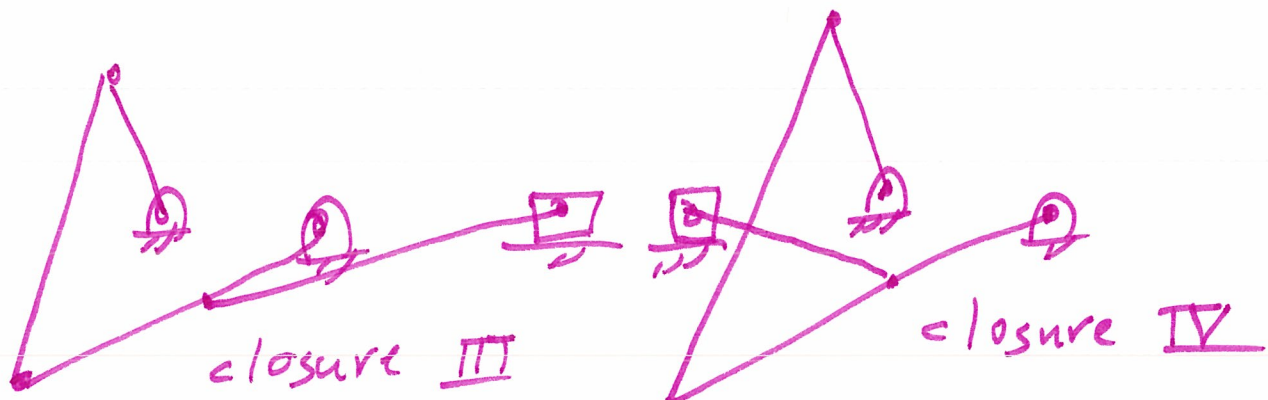
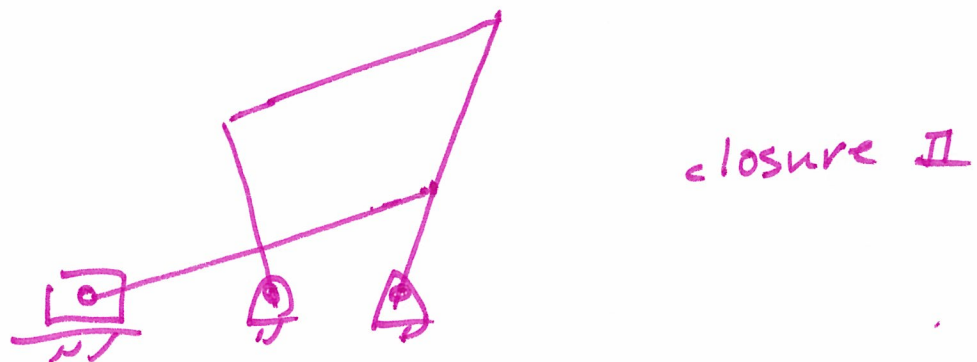
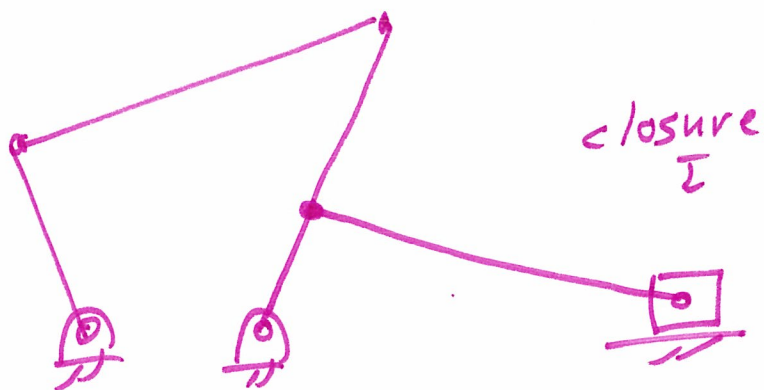
Crank-Slider (compressor)



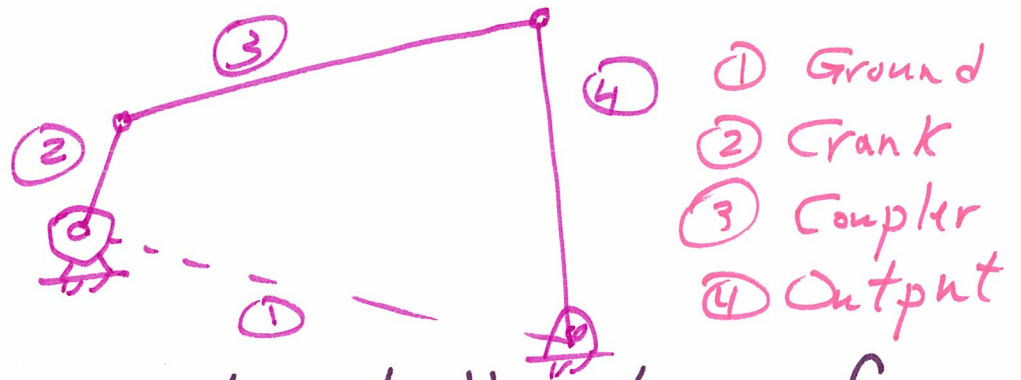
Example
RRPR



1 closure



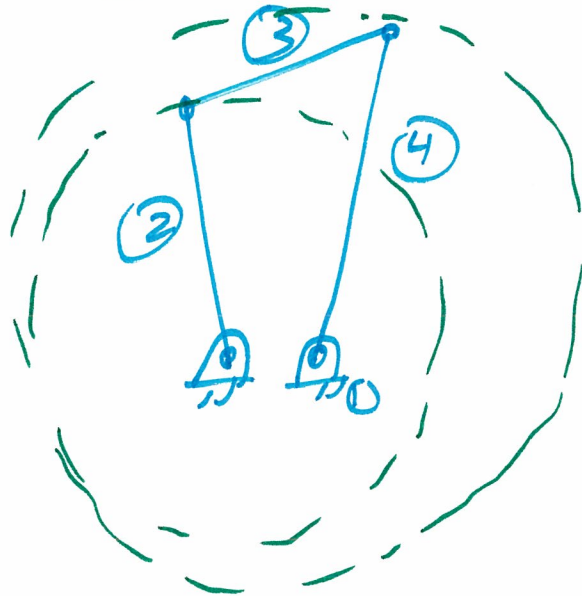
4-Bar Mechanism



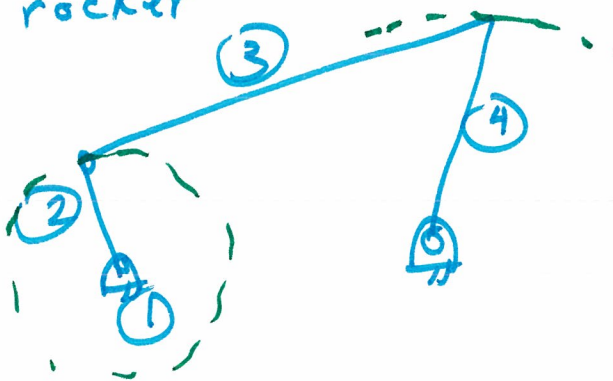
Classify according to the type of motion

* Crank-crank (Drag) (Drag link)

② & ④ rotate 360°



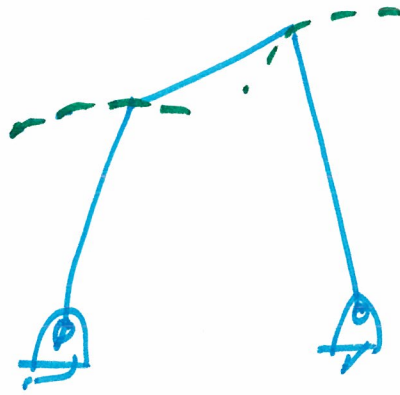
* Crank-rocker



② rotates 360°
④ oscillates

* Rocker-Rocker

② & ④ oscillate



60°

5

H. W.

Construct a 4-bar mechanism
with these dimensions:

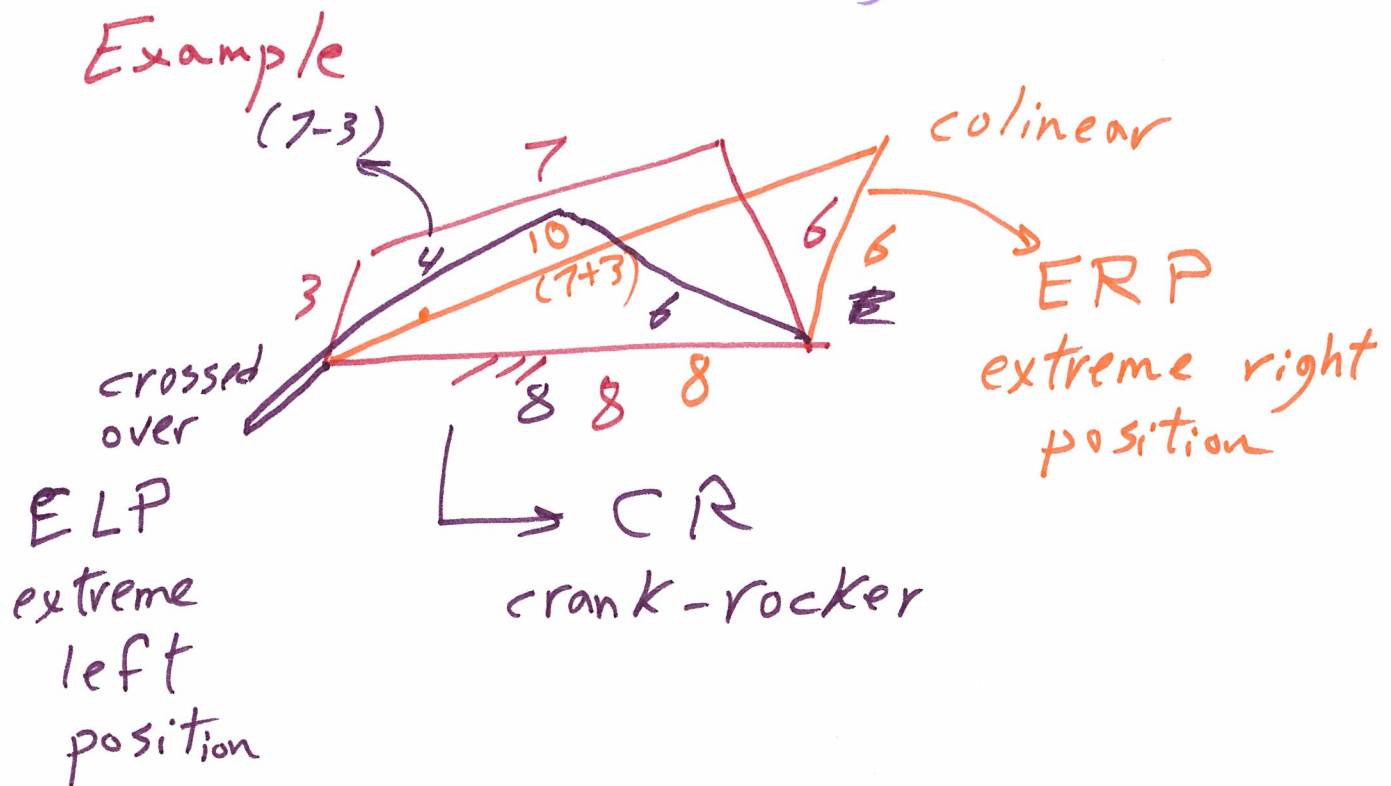
3 8 6 7

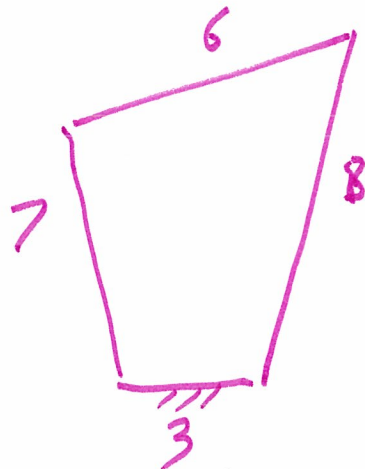
Use any material provided
that the motion is not
interrupted

4. Bar Mechanism Types

↳ Motion classification
is based on identifying motion
limits of the mechanism

Change of Quadrilateral
into Triangle

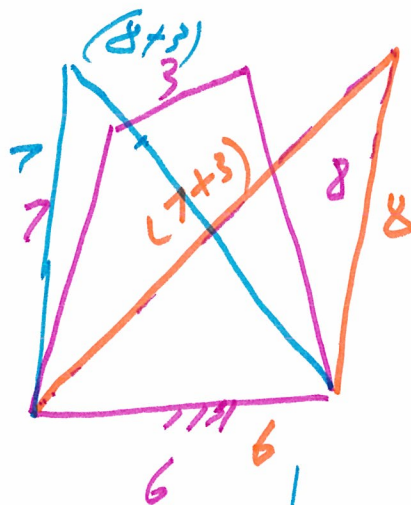




$(7+6), 8, 3$
do not constitute
triangle

$(7-6), 8, 3$
" " "

↘ CC
crank-crank



$(7+3), 8, 6$
constitute a triangle

$(8+3), 7, 6$
" " "

↘ RR
rocker-rocker

Grashof Criteria

If the sum of the longest & shortest links $<$ the sum of the two other links, then the 4-bar mechanism is,

- Crank-crank if the shortest is the fixed
- Crank-rocker " " " " "
- Rocker-rocker " " " " "
- coupler

If the mechanism does not satisfy the above inequality, it is rocker-rocker

Example:

Given 4-bar mechanism with the following dimensions 3 7 8 6.

Link 3 is the crank.

$$8 + 3 < 7 + 6 \rightarrow \text{inequality is satisfied}$$

$\rightarrow$ CR (3 is the crank)

Link 3 is fixed

CC (3 is fixed)

Example

4-bar with these lengths:

3 3 7 6

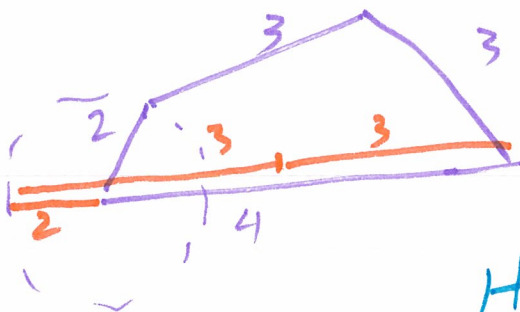
$7+3 > 6+3 \rightarrow$ inequality is
10 9 not satisfied
RR

~~3 3 7 5~~
1 2 7 3

Special case $\rightarrow$ inequality becomes
equality

2 4 3 3

$2+4 = 3+3$
6 6



change case
 $\rightarrow$ RR

H.W
2.15

2.19

2.22

2.26