Today:

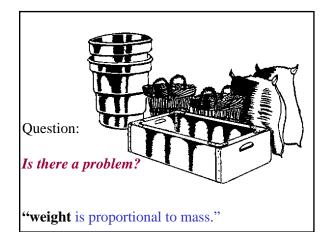
Chapter 6 continued: Dimensions and Units

English units of measurement

A system of weights and measures used in a few nations, the only major industrial one being the United States. It actually consists of two related systems—the U.S. Customary System of units, used in the United States and dependencies, and the British Imperial System.

Units of Weight

The pound (lb) is the basic unit of weight (which is proportional to mass) (how?). Within the English units of measurement there are three different systems of weights. In the avoirdupois system, the most widely used of the three, the pound is divided into 16 ounces (oz) and the ounce into 16 drams. The ton, used to measure large masses, is equal to 2,000 lb (short ton) or 2,240 lb (long ton). In Great Britain the stone, equal to 14 lb, is also used.



Answer: You need to be aware of

the law governing that proportionality: Newton's Law

Force = Mass* Acceleration

Question:

Is there a problem?

"weight is proportional to mass."

Force = Mass* Acceleration

Acceleration is NOT a constant, mass is.

Even on earth, $g = 9.81 \text{ m/s}^2$ is NOT constant, but varies with latitude and elevation.

"weight is proportional to mass."

Another problem arises from the common intermingling of the terms "mass" and "weight", as in:

"How much does a pound of mass weigh?"

Or:

"If you don't know whether it's poundmass or pound-weight, simply say pounds." A mass is NEVER a "weight".

Force = Mass* Acceleration

"Weight" = Force

"Weight" = Force

...because on earth all masses are exposed to gravity. So

Weight =m * g

The notion of 'weight' is not very useful in engineering, because many situations are not static.

Forces in SI Units

 $1N = 1 \text{ kg* } 1\text{m/s}^2$

When SI units are used, the factor g_c is 1. There is no need for g_c in the SI system.

Forces in US Customary Units

Force is a Basic unit Mass becomes a derived unit: 1 lb-mass (lbm)

11bf = 11bm*g or 1 lbm = 11bf/gWhere g is approx. 32.2 ft/s^2

Conversions

Example: convert meters to miles. Conversion factor: 1 mile = 1609 m 3200m =? miles

Answer:

3200m = 3200m* 1mi/1609m= 3200/1609 mi = 1.989 miles

Conversions

In class exercise: convert feet to miles.

Conversion factor: 1 mile = 5280 ft

9800 ft = ? miles

Conversions

In class exercise (speed): convert miles/hour

to feet/second.

Conversion factor: 1 mile = 5280 ft

45 mph = ??? ft/s

In class exercise (speed): convert miles/hour

to feet/second.

Conversion factor: 1 mile = 5280 ft

45 mph = ??? ft/s

Step by step procedure:

 $45mph = \frac{45mi}{1hr}$

We can multiply by

$$1 = \frac{5280 ft}{1mi}$$

In class exercise (speed): convert miles/hour

to feet/second.

Conversion factor: 1 mile = 5280 ft

45 mph = ??? ft/s

Step 2:

 $45mph = \frac{45mi}{1hr} * \frac{5280\,ft}{1mi}$ Thus:

In class exercise (speed): convert miles/hour to feet/second.

Conversion factor: 1 mile = 5280 ft

45 mph = ??? ft/s

Step 3:

We repeat the process for the time:

$$45mph = \frac{45mi}{1hr} * \frac{5280\,ft}{1mi}$$

Multiply by $1 = \frac{1hr}{3600s}$

In class exercise (speed): convert miles/hour

to feet/second.

Conversion factor: 1 mile = 5280 ft

45 mph = ??? ft/s

Step 4:

We get: $45mph = \frac{45mi}{1hr} * \frac{5280 ft}{1mi} * \frac{1hr}{3600s}$

We can now simplify the fractions.

The units mi and hr cancel.

In class exercise (speed): convert miles/hour to feet/second. 45 mph = ??? ft/s

Step 5:

We get:
$$45mph = 45*\frac{5280 ft}{3600 s} = 66 \frac{ft}{s}$$

Plausibility check:

The resulting units *must* be distance/time. The resulting numbers *must* be consistent with the original question.

Conversions

Pressure = Force per unit area

In class:

Convert 35,000 Pa to psi, using basic units such as feet and pounds-force.

In class:

Convert 35,000 Pa to psi, using basic units such as feet and pounds-force.

Definitions:

$$1Pa = \frac{1N}{m^2}$$

$$1Pa = \frac{1N}{m^2} \qquad 1psi = \frac{1lbf}{in^2}$$

In class:

Convert 35,000 Pa to psi, using basic units such as feet and pounds-force.

Solution:

$$35000Pa = \frac{35000N}{m^2} * \frac{0.2248lbf}{1N} * \frac{1m^2}{39.37^2in^2}$$

In class:

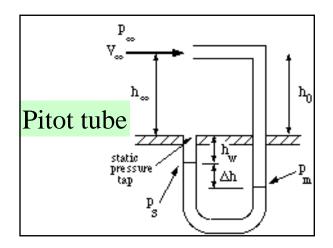
Convert 35,000 Pa to psi, using basic units such as feet and pounds-force.

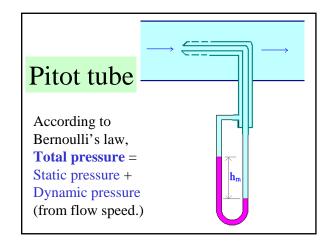
Solution:

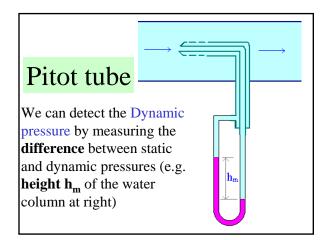
Thus:
$$35000Pa = 35000 * \frac{0.2248lbf}{39.37^2in^2} = 5.076psi$$

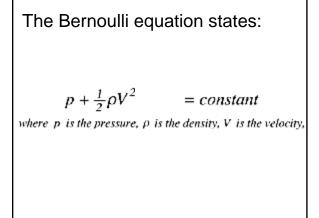
Some measurements involve multiple units and conversions

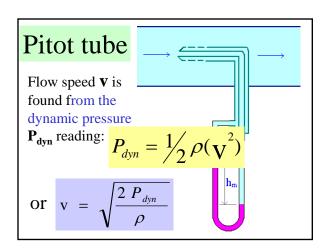
Example: Flow speed measurement with a Pitot tube

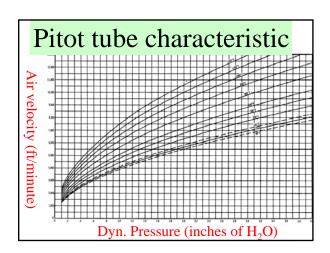












$$V = \sqrt{\frac{2 P_{dyn}}{\rho}}$$

In class: Pitot tube measurement analysis

Given: $P_{dyn} = 500 \text{ Pa}$

 $\rho_{Air} \ = 1.2 \ kg/m^3 \ at \ 1.01*10^5 \ Pa$

Determine the air velocity in m/s

$$V = \sqrt{\frac{2 P_{dyn}}{\rho}}$$
Inserting:

Inserting: $P_{dyn} = 500 \text{ Pa}$

 $\rho_{Air} = 1.2 \ kg/m^3$

gives

$$v = \sqrt{\frac{2 * 500}{1.2} \frac{N}{m^2} \frac{m^3}{kg}}$$

SI
$$v = \sqrt{\frac{2 * 500}{1.2} \frac{N}{m^2} \frac{m^3}{kg}}$$

We substitute: 1N with 1 kgm/s²

$$v = \sqrt{\frac{2 * 500}{1.2} \frac{N}{m^2} \frac{m^3}{kg} \frac{1 \, kgm}{1 \, N * s^2}}$$

Simplification gives:

$$v = \sqrt{833 \frac{m^2}{s^2}} = 28.9 \frac{m}{s}$$

SI
$$v = \sqrt{\frac{2 P_{dyn} * g_c}{\rho}}$$
 US Cust. $v = \sqrt{\frac{2 P_{dyn} * g_c}{\rho}}$

In class: Pitot tube measurement analysis

Given: $P_{dyn} = 19 lbf/ft^2$

 $\rho_{Air}~=0.0735~lbm/ft^3~at~14.7~psia$

Determine the air velocity in ft/s

US Customary example

$$\mathbf{v} = \sqrt{\frac{2P_{dyn} * g_c}{\rho}}$$

Inserting: $P_{dyn} = 19 \text{ lbf/ft}^2$

 $\rho_{Air} = 0.0735 \ lbm/ft^3$

$$v = \sqrt{\frac{2*19lbf}{ft^2} \frac{32.2}{1} \frac{lbm*ft}{lbf*s^2} \frac{ft^3}{0.0735lbm}}$$

$$v = \sqrt{\frac{2*19lbf}{ft^2} \frac{32.2}{1} \frac{lbm*ft}{lbf*s^2} \frac{ft^3}{0.0735lbm}}$$

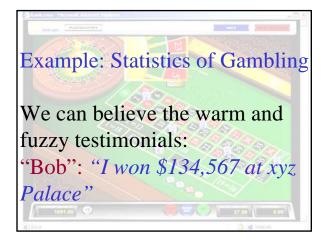
Simplification gives:

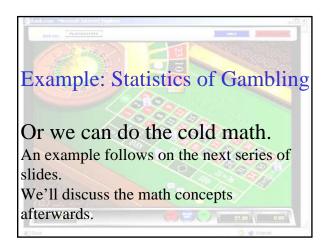
$$v = \sqrt{16648 \frac{ft^2}{s^2}} = 129 \frac{ft}{s}$$

Chapter 8

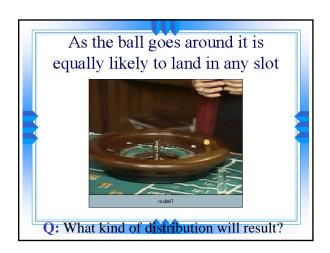
Statistics



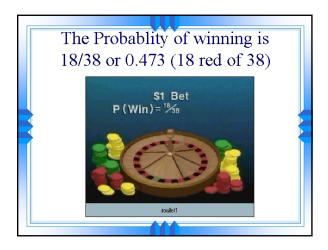


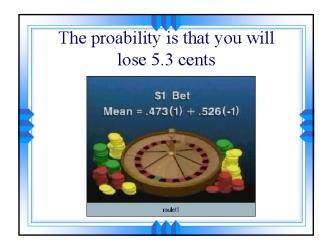








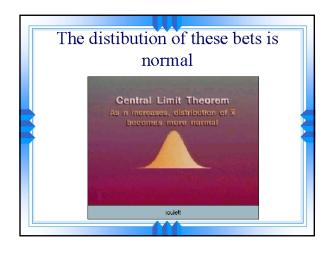


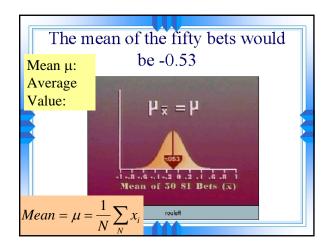












Mean

$$\bar{\mathbf{x}} = (\sum x_{\mathbf{I}}) / n$$

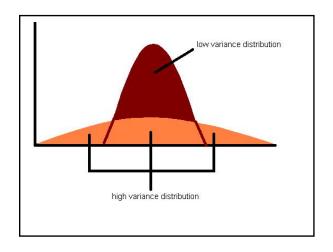
Variance

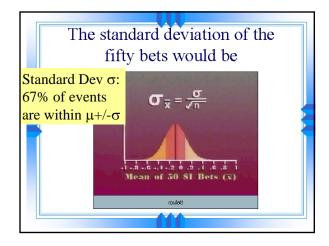
$$\sigma^{2} = \sum \frac{(x_{i} - \overline{x})}{n - 1}$$
Where
$$\sigma^{2} = \text{Variance}$$

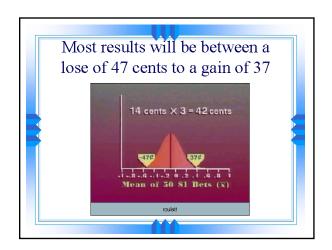
$$x_{I} = \text{Each item}$$

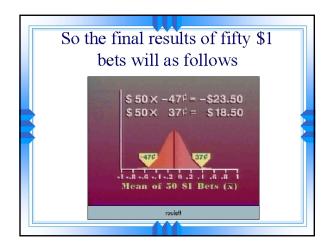
$$\bar{x} = \text{sample mean}$$

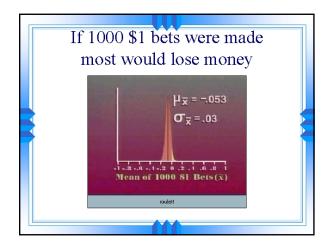
$$n = \text{sample size}$$

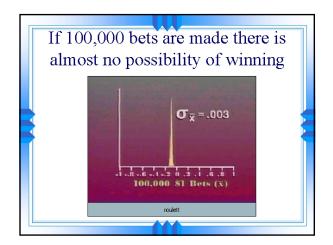












The preceding analysis did not consider the fact that the casino limits the player's capital.
All casino tables carry a sign e.g. "minimum bet \$5 maximum bet \$500"

Without the sign, a player could recover from losing streaks by doubling each losing bet, to lose only the predicted 5%.

The sign prevents the player from recovery at the point of maximum profit to the casino.

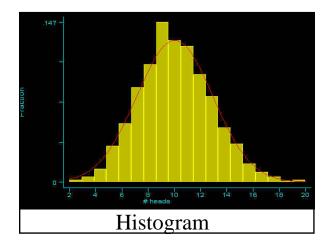
The average table game winnings at Nevada casinos are 15% of wagered amounts.

Statistical Analysis Example

Playing heads or tails. We toss 20 coins each time, and count the numbers of heads.

# heads out of 20			
tossed	Freq.	Percent	Cum.
2	2	0.20	0.20
3	5	0.50	0.70
4	12	1.20	1.90
5	33	3.30	5.20
6	54	5.40	10.60
7	87	8.70	19.30
8	108	10.80	30.10
9	147	14.70	44.80
10	130	13.00	57.80
11	125	12.50	70.30
12	99	9.90	80.20
13	79	7.90	88.10
14	50	5.00	93.10
15	35	3.50	96.60
16	17	1.70	98.30
17	9	0.90	99.20
18	5	0.50	99.70
19	1	0.10	99.80
20	2	0.20	100.00
Total	1000	100.00	

We can plot the number of heads counted in each of the 20 classes vs. the frequency of occurrence. This plot is called a histogram.



The histograms of random distributions exhibit the familiar Gaussian "bell curve" shape.

Many distributions are "biased" by deterministic factors. Statisticians can detect such biases and point to their causes.

Some examples follow.